

# **The extended Multiple Discrete-Continuous Extreme Value (MDCEV) Model (multiple car case)**

## **Contents**

- 1. Scope and motivation**
- 2. Method**
- 3. Basic idea behind the model**
- 4. The model (multiple car case)**
- 5. Simulation results (two car case)**
- 6. Existing model and key results**
- 7. Discussion**

Presentation at STRC Ascona on 25 April 2013  
Reto Tanner, [retanner@gmx.ch](mailto:retanner@gmx.ch)

# 1. Scope and motivation

Examining the effects of

i.) a fuel tax

ii.) a tax on car ownership

on

a.) aggregate annual mileage of cars

b.) car ownership and the proportion of carless households

**c.) car choice with respect to car type and thus to fuel efficiency (new!)**

## 2. Method

### Discrete Choice Model

$$\max_i U_i = V_i + \varepsilon_i$$

$U_i$  : Utility of product type  $i$

$V_i$  : Deterministic component

$V_i = V_i(x_i, s)$  “*arbitrary*” utility function, of...

$x_i$  : Product properties

$s$  : Sociodemographic attributes of the household

$\varepsilon_i$  : Stochastic component. (Represents unobserved product properties, etc.)

***“Choose the product type  $i$  that provides the highest utility!”***

## Discrete-continuous Choice Model (MDCEV)

*“Which car(s) are owned and how many km’s they are driven?”*

$$\underbrace{\max_{S_i} u_i = u(x, \varepsilon); x, \varepsilon \in S_i, S_i \subset R_n, \text{ eg.: } S_i = (x_1, 0, x_3, x_4, 0, x_6)}_{\text{Preferences}} \quad \text{s.t.} \quad \underbrace{\text{economic constraints}}_{\text{income and prices}}$$

$x = x_i(y, p, \varepsilon); p, \varepsilon \in S_i$ 
  
 Optimal consumption (Mashallian Demand Function)
   
  
 $u_i = u(x_i, \varepsilon)$ 
  
 Utility

$u_i = u(x_i, \varepsilon)$  *microeconomic* utility function,

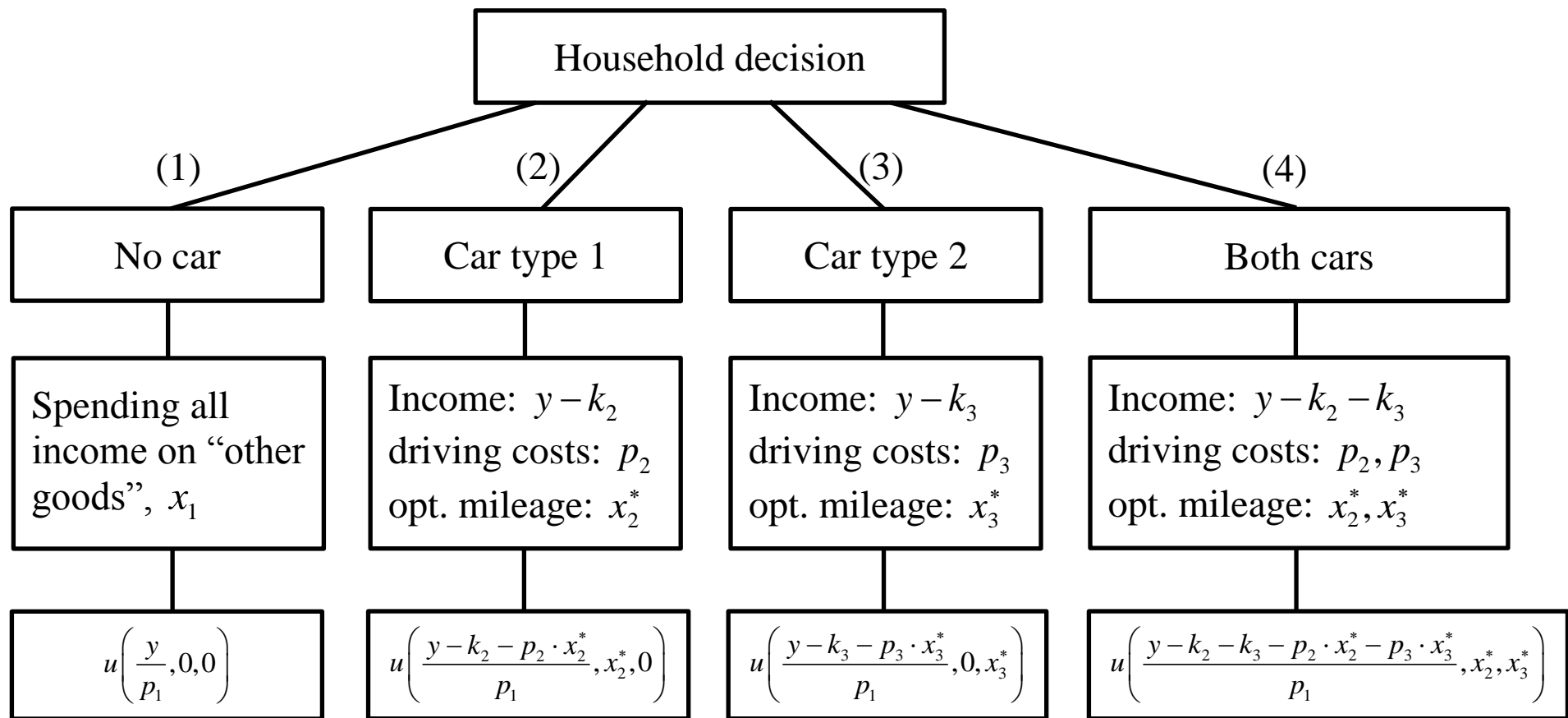
$\varepsilon_i$  : Stochastic component. (Represents unobserved consumer preferences, etc.)

*“Choose the combination of car(s)  $S_i$  that yields the highest utility!”*

## Remarks:

- *Why a **microeconomic** utility function?*
  - *I must relate the utility level to a driving distance*
  - *I want to make use of the properties of the microeconomic theory, here:*
    - *“Normal good”:*
      - *Demand increases with income ...*
      - *... and decreases with its own price*
    - *Imposes restrictions on the demand function*
  - *Demand functions are economically consistent*
- *The utility function has a stochastic component, thus the Marshallian demand function is stochastic too*
- *This modelling framework clearly separates the effect of changes of the preferences and changes in the economic environment (income and prices)*

### 3. Basic idea behind the model



**Choice:**  $\arg \max_{i=1..4} (u_{(1)}, u_{(2)}, u_{(3)}, u_{(4)})$

## 4. The model (multiple car case)

$$\max_{x_1, x_2, \dots, x_{n+1}} u(x_1, x_2, \dots, x_{n+1}) = (x_1 + a_1)^d + \sum_{i=1}^n \exp(m_{i+1} + \beta \cdot \zeta_{i+1}) \cdot (x_{i+1} + a_{i+1})^d$$

$$\text{Subject to: } y = \sum_{i=1}^n I(x_{i+1} > 0) \cdot k_{i+1} + p_1 \cdot x_1 + \sum_{i=1}^n p_{i+1} \cdot x_{i+1},$$

for each possible combination of car choice, e.g.  $(x_1, x_2, 0, x_4, 0, \dots, 0)$ .

$k_{i+1}$ : Fixed costs of car type  $i$

$x_{i+1}$ : Car-km with car type  $i$ ,  $i = 1..n$

$x_1$ : Composite good: All other goods (housing, holidays, consumption goods, ...)

$p_{i+1}$ : Marginal costs of a car-km of car type  $i$  (note:  $p_1 = 1$ )

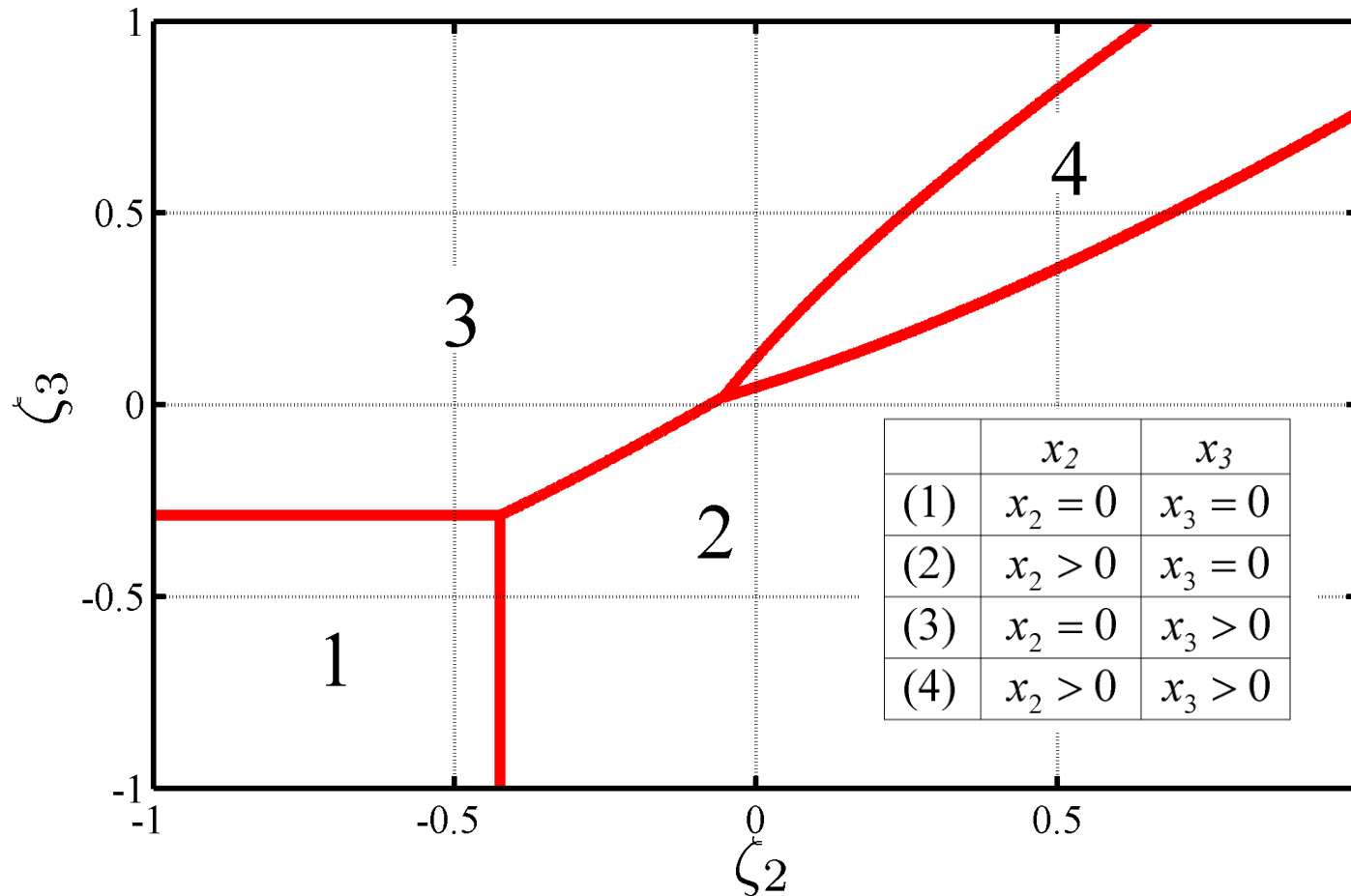
$m_{i+1} + \beta \cdot \zeta_{i+1}$ : Relative preference for driving car type  $i$

$\beta \cdot \zeta_{i+1}$ : Stochastic component of the relative preference for driving a certain car

$\zeta_i$ : Standard-Gumbel distributed

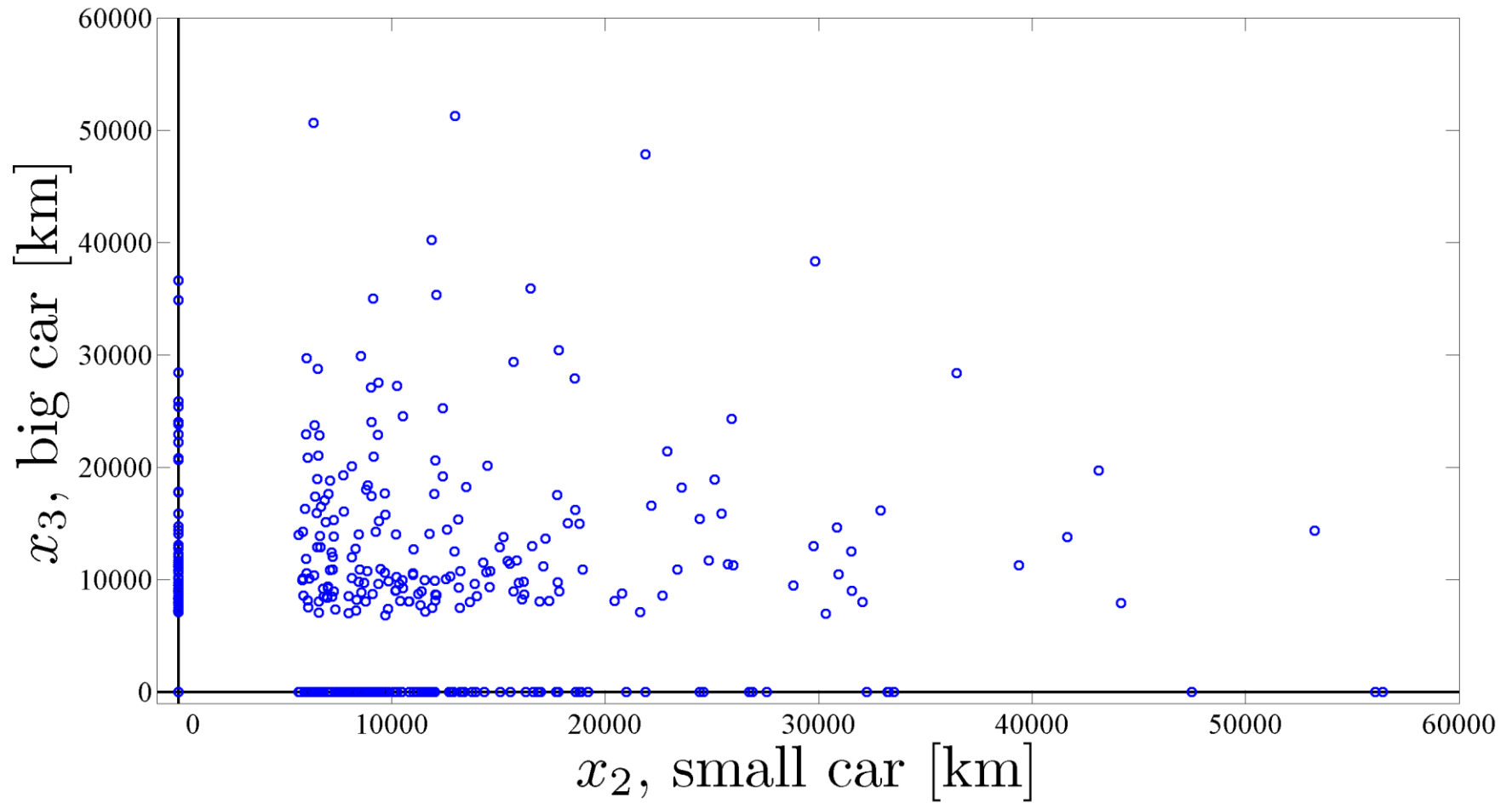
Example:  $m_i = \gamma_{i,0} + \gamma_{i,1} \cdot rural$ , where  $rural = 1$  if the household lives in a rural area

## 5. Simulation results (two car case)

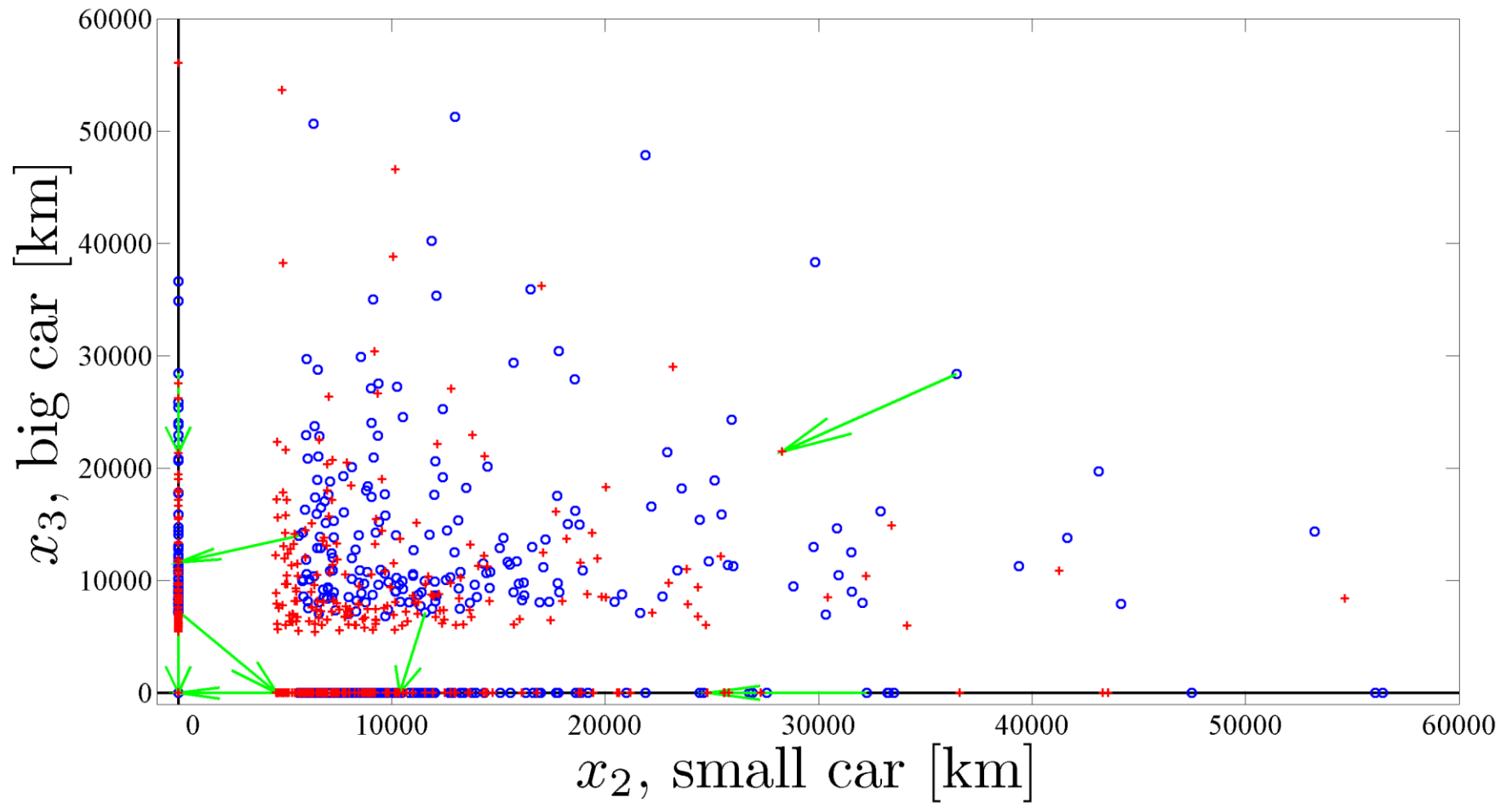


**Figure 1:** Preference for certain car types and choice of car combinations

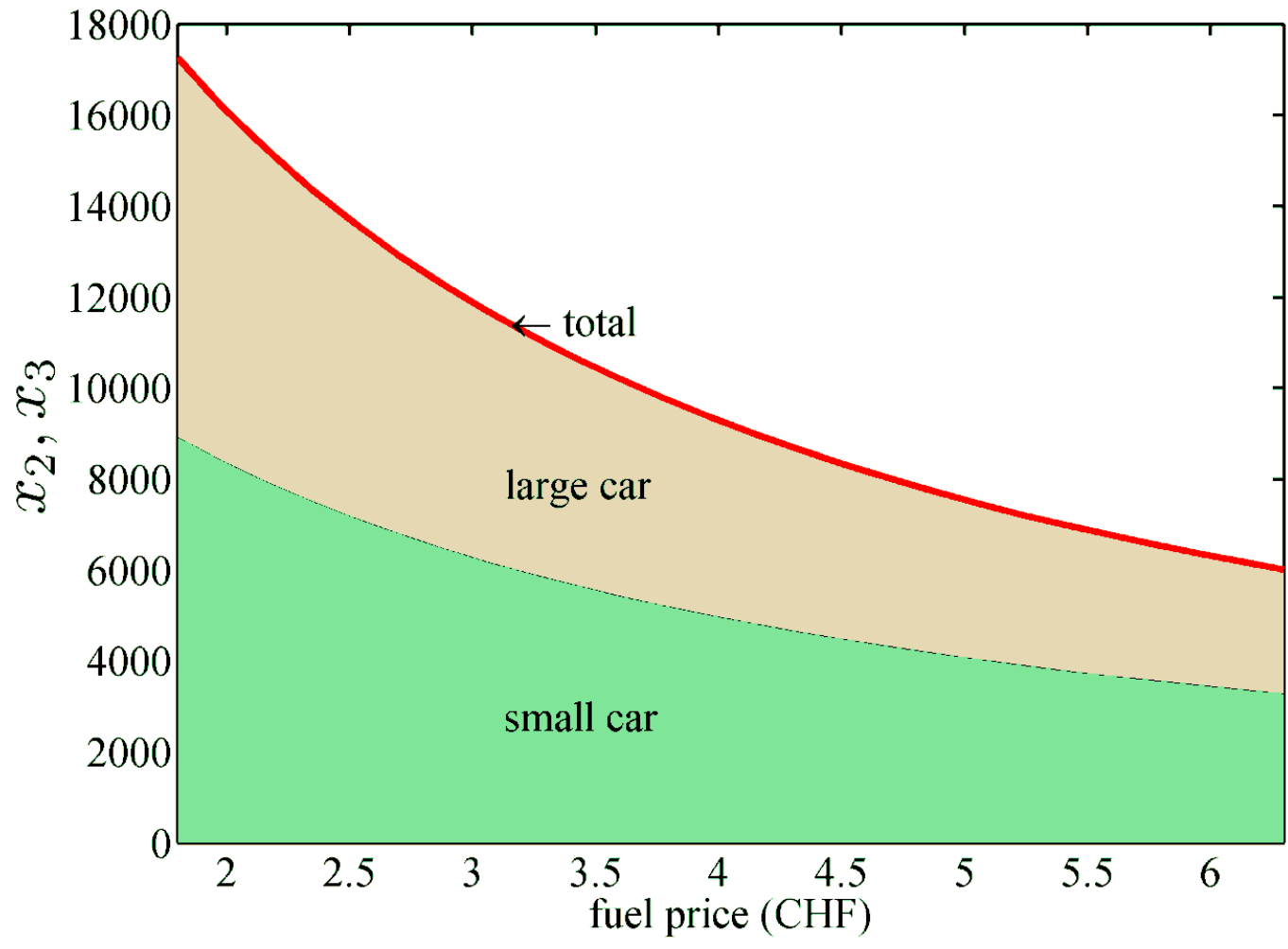




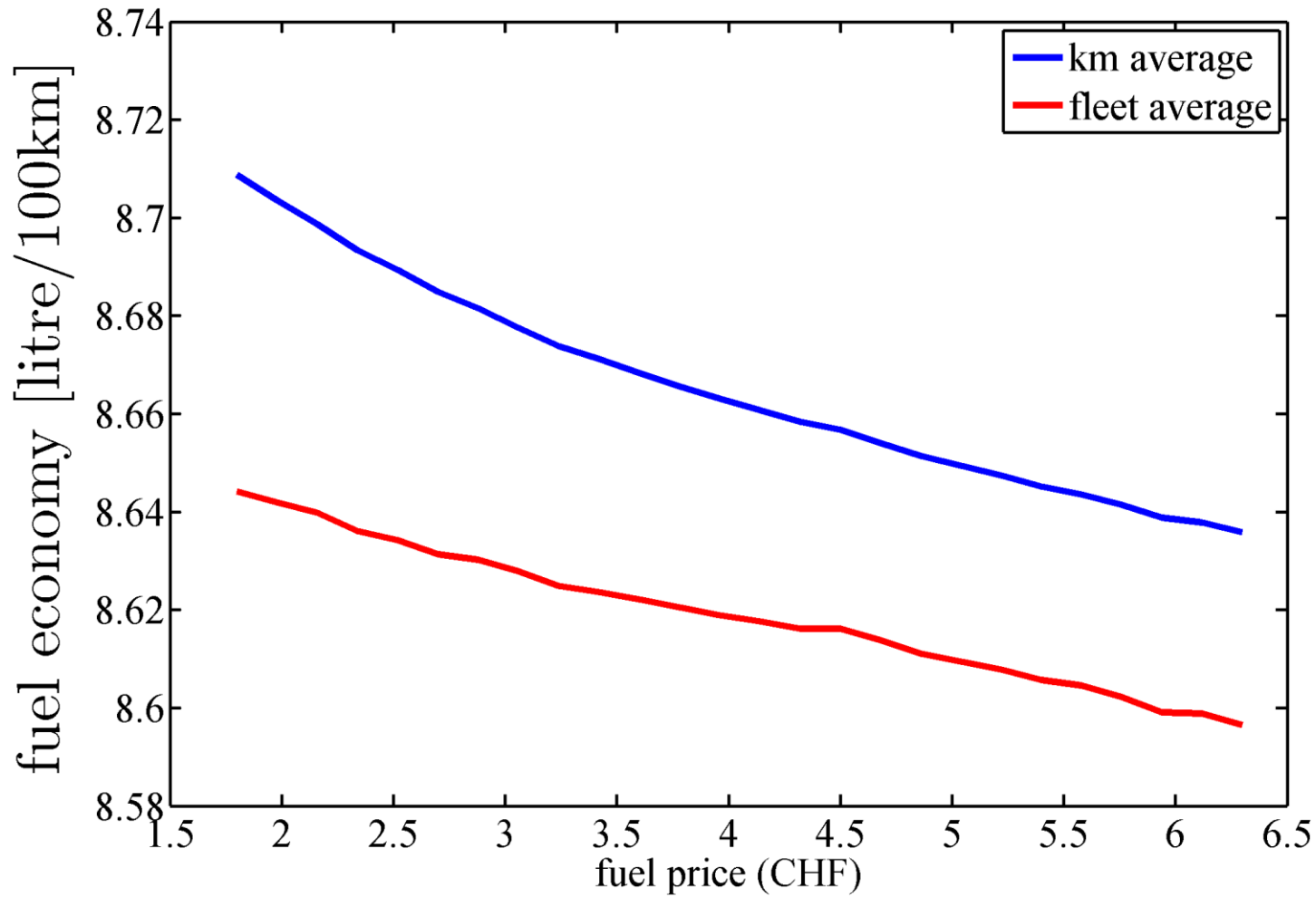
**Figure 2:** Simulated density function of a household with an annual income of CHF 84,000



**Figure 3:** Simulated density function when the fuel price increases by 50%



**Figure 4:** Change in annual mileage when the fuel price increases



**Figure 5:** Change in annual mileage when the fuel price increases

## 6. Existing model and key results

- The existing model – the extended MDCEV model (**one car case**) – captures only one car type
- The key results are:
  - i.) the main effect of a fuel tax on the aggregate annual mileage is that “heavy users” will decrease the distance driven and not that households will sell the car
  - ii.) the effect of a fuel tax on the aggregate annual mileage is much greater than the effect of a tax on car ownership – per unit of tax revenue

## 7. Discussion

- Estimation routine?
- Results driven by the specification of the model structure?
- Substitutionability between car types mapped by the model?